

Math 315 Sections 1 and 2
16–17 March 2007
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Test 2
Show relevant work!

Name _____

1. Let $f : A \rightarrow \mathbb{R}$ be a real-valued function. Give the sequence definition of continuity and the $\varepsilon - \delta$ definition of continuity.
2. Prove that a closed interval has the property that if it is covered by a collection of open sets, then some finite sub-collection of the open sets covers.
3. Given f and g are differentiable functions with domain all real numbers. If $g(x) \neq 0$, prove that $F(x) = \frac{f(x)}{g(x)}$ is differentiable at c and find the derivative
4. State and prove the Mean Value Theorem.

5. Prove the uniform limit of continuous functions is continuous.

6. Show that if f is a differentiable, real-valued function defined for all real numbers with a bounded derivative, then f is uniformly continuous.

7. Show that $f(x) = \frac{1}{x^2}$ is not uniformly continuous on $(0,1]$.

8. Prove or give a counterexample. If $f_n \rightarrow f$ point-wise on an interval and each f_n is increasing, then f is also increasing.